Hybrid DSGE models with financial frictions for macroprudential policy and forecasting *

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Abstract

The financial crisis has shown that neither VAR nor simple DSGE macro-modelling is fully ready to deal explicitly with the issue of financial frictions and stability that play an important role in modern business cycle. In particular, DSGE models that incorporate financial frictions could deal with the transmission mechanism of standard shocks changes and how monetary policy is affected by the presence of frictions, as well as with optimal macroprudential policies and the impact of capital requirements. In this paper, we conduct a comparative empirical analysis of the out-of-sample predictive performance of simple and hybrid DSGE models against standard VARs, Bayesian VARs and Factor Augmented VARs, using datasets from the US economy. We employ advanced Bayesian techniques in estimating and forecasting the models. From a modelling point of view we focus on the interaction of frictions both at firms' level and in the banking sector in order to examine the transmission mechanism of the shocks and to reflect on the response of the monetary policy to increases in interest rate spreads, especially after the financial crisis. Overall, in this study a first attempt is made to find macro-financial models which are able to reflect reality better.

JEL Classification: C32, C11, C15

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1 Introduction

Dynamic stochastic general equilibrium (DSGE) models are widely used among central banks and institutions as well as in the academia in order to test alternative monetary, fiscal and macroprudential policies under different scenarios. However, the financial crisis shows that the workhorse of contemporary DSGE modelling is not fully ready to deal explicitly with the issue of credit frictions and financial stability, which play an important role in modern business cycle. In recent times there have been some efforts to model financial factors: Goodfriend and McCallum (2007), Christiano, Motto and Rostagno (2010), Curdía and Woodford (2010), Gerali, Neri, Sessa and Signoretti (2010), Gertler and Kiyotaki (2010) and Gertler and Karadi (2011) constitute some promising attempts to study the effects of financial intermediation on business cycle fluctuations and policy design. In particular, DSGE models with financial frictions could deal with many issues, such as: (i) the effect of financial shocks on real variables, (ii) how the transmission mechanism of "standard shocks" changes in presence of imperfect capital markets (iii) how optimal monetary policy is affected by the presence of financial frictions and (iv) optimal macroprudential policies and the impact of capital requirements. In the literature there are three main strands of research on financial frictions: (i) financial frictions at the level of firms, following the seminal contribution of Bernanke et al. (1999) (BGG), (ii) frictions at the level of households in the form of collateral constraint introduced by Kiyotaki and Moore (1997) and Iacoviello (2005) and (iii) frictions at the level of financial intermediaries as in Gertler and Karadi (2011). These different modelling techniques capture the problem of asymmetric information between borrowers and lenders, which leads to a constraint in the borrowers' ability to obtain credit.

The dynamic stochastic general equilibrium models appear to be particularly suited for evaluating the consequences of alternative macroeconomic policies, as shown in the works of Smets and Wouters (2003, 2004), Del Negro and Schorfheide (2004), Adolfson et al. (2008) and Christiano et al. (2005). However, the calibrated dynamic stochastic general equilibrium (DSGE) models face many important challenges such as the fragility of parameter estimates, statistical fit and the weak reliability of policy predictions as reported in Stock and Watson (2001), Ireland (2004) and Schorfheide (2010). In recent years Bayesian estimation of DSGE models has become popular for many reasons, mainly because it is a system-based estimation approach that offers the advantage of incorporating assumptions about the parameters based on economic theory. Recently, increasing efforts have been undertaken to use DSGE models for forecasting. DSGE models were not considered as forecasting tools until the works of Smets and Wouters (2003, 2004) on the predictability of DSGE models compared to alternative non-structural models. In the macro-econometric literature, hybrid or mixture DSGE models have become popular for dealing with some of the model misspecifications as well as the trade-off between theoretical coherence and empirical fit (Schorfheide, 2010). They are categorized in additive hybrid models and hierarchical hybrid models. The hybrid models provide a complete analysis of the data law of motion and better capture the dynamic properties of the DSGE models. In the recent literature, different attempts of hybrid models have been introduced for solving, estimating and forecasting with DSGEs. Sargent (1989) and Altug (1989) proposed augmenting a DSGE model with measurement error terms that follow a first order autoregressive process, known as the DSGE-AR approach. Ireland (2004) proposed a method that is similar to the DSGE-AR, but imposing no restriction on the measurement errors, assuming that residuals follow a first-order vector autoregression (DSGE-AR à l'Ireland). A different approach called DSGE-VAR was proposed by Del Negro and Schorfheide (2004) and was based on the works DeJong et al. (1996) and Ingram and Whiteman (1994). The main idea behind the DSGE-VAR is the use of the VAR representation as an econometric tool for empirical validation, combining prior information derived from the DSGE model in estimation. However, it has several problems. One of the main problems in finding a statistical representation for the data by using a VAR, is overfitting due to the inclusion of too many lags and too many variables, some of which may be insignificant. The problem of overfitting results in multicollinearity and loss of degrees of freedom, leading to inefficient estimates and large out-of-sample forecasting errors. It is possible to overcome this problem by using the wellknown "Minnesota" priors (Doan et al., 1984). The use of "Minnesota" priors has been proposed to shrink the parameters space and thus overcome the curse of dimensionality. Following this idea in

combining the DSGE model information and the VAR representation, two alternative econometric tools have been also introduced: the DSGE-FAVAR (Consolo *et al.*, 2009) and the Augmented VAR-DSGE model (Fernández-de-Córdoba and Torres, 2010). The main idea behind the Factor Augmented DSGE (DSGE-FAVAR) is the use of factors to improve the statistical identification in validating the models. Consequently, the VAR representation is replaced by a FAVAR model as the statistical benchmark.

In this work, we conduct an exhaustive empirical exercise that includes the comparison of the outof-sample predictive performance of estimated simple and hybrid DSGE models with that of standard VARs, Bayesian VARs and Factor Augmented VARs as well as DSGE-VAR and Factor Augmented DSGE models estimated on the same data set for the US economy. The DSGE model is obtained by augmenting the small-scale model with financial frictions, following Christiano et al. (2009) and Del Negro and Schorfheide (2012). We start considering the Smets-Wouters model with financial frictions proposed by Del Negro and Schorfheide (2012). After the recent financial crisis, the spread is a key variable measured as the annualized Moody's Seasoned BAA corporate bond yield spread over the 10-Year Treasury note yield at constant maturity. As in Christiano, Motto and Rostagno (2009) we include the spread to reflect on the response of the monetary policy to increases in interest rate spreads. The variety of estimation techniques employed makes it possible to compare estimations according to different criteria: analyzing the posterior means of key parameters, calculating the marginal data density, building Bayes Factors and forecasting comparison. The main purpose of this paper is to compare different econometrics strategies in evaluating a DSGE economy, but mainly to stress the importance of considering financial variables in particular for the US economy during and after the recent financial crisis. We focus on many different specifications of the DSGE models, i.e., the simple DSGE, the DSGE-VAR and specifically on the Factor Augmented DSGE (DSGE-FAVAR) model with emphasis on Bayesian estimation. We use time series data from 1960:Q4 to 2010:Q4 for the real GDP, the harmonized Consumer Price Index, the nominal short-term federal funds interest rate and the yield spread, and we produce their forecasts for the out-of-sample testing period 1997:Q1-2010:Q4. The motivation comes from a group of recent papers that compares the forecasting performance of DSGE against VAR models, e.g., Smets and Wouters (2004), Ireland (2004), Del Negro and Schorfheide (2004), Del Negro et al. (2007), Adolfson et al. (2008), among others. The remainder of this paper is organized as follows. Section 2 describes the standard and Bayesian VAR as well as the Factor Augmented VAR model. In section 3 the proposed DSGE model with financial frictions is analyzed, and the hybrid DSGE-VAR and DSGE-FAVAR models are described in detail. In section 4 the data are described and the empirical results of the comparative forecasting evaluation are illustrated and analyzed. Finally, section 5 concludes.

2 Vector Autoregressive Models

The standard unrestricted VAR as suggested by Sims (1980) has the following compact format

$$\mathbf{Y}_t = \mathbf{X}_t \mathbf{\Phi} + \mathbf{U} \tag{1}$$

where \mathbf{Y}_t is a $(T \times n)$ matrix with rows Y'_t , and \mathbf{X} is a $(T \times k)$ matrix (k = 1 + np, p = number of lags) with rows $X'_t = [1, Y'_{t-1}, ..., Y'_{t-p}]$. \mathbf{U} is a $(T \times n)$ matrix with rows $u'_t, \mathbf{\Phi}$ is a $(k \times n) = [\Phi_0, \Phi_1, ..., \Phi_p]'$, while the one-step ahead forecast errors u_t have a multivariate $N(0, \Sigma_u)$ conditional on past observations of Y.

2.1 Bayesian VAR

One of main problems in using VAR models is that many parameters need to be estimated, although some of them may be insignificant. Instead of eliminating longer lags, the BVAR imposes restrictions on these coefficients by assuming that they are more likely to be near zero than the coefficients on shorter lags (Litterman, 1981; Doan *et al.*, 1984; Todd, 1984; Litterman, 1986; Spencer, 1993). Obviously, if there are strong effects from less important variables, the data can counter this assumption. Usually, the restrictions are imposed by specifying normal prior distributions with zero means and small standard deviations for all coefficients, with a decreasing standard deviation as the lags increase. The only exception is the coefficient on a variable's first lag that has a mean of unity. Litterman (1981) used a diffuse prior for the constant. The means of the prior are popularly called the "Minnesota Priors" due to the development of the idea at the University of Minnesota and the Federal Reserve Bank at Minneapolis¹. Formally speaking, these prior means can be written as follows

$$\Phi_i \sim N(1, \sigma_{\Phi_i}^2)$$
 and $\Phi_j \sim N(0, \sigma_{\Phi_i}^2)$, (2)

where Φ_i denotes the coefficients associated with the lagged dependent variables in each equation of the VAR, while Φ_j represents any other coefficient. The prior variances $\sigma_{\Phi_i}^2$ and $\sigma_{\Phi_j}^2$ specify the uncertainty of the prior means, $\Phi_i = 1$ and $\Phi_j = 0$, respectively. In this study, we impose their prior mean on the first own lag for variables in growth rate, such as a white noise setting (Del Negro and Schorfheide 2004; Adolfson *et al.* 2007; Banbura *et al.* 2010). Instead, for level variables, we use the classical Minnesota prior (Del Negro and Schorfheide 2004). The specification of the standard deviation of the distribution of the prior imposed on variable j in equation i at lag m, for all i, j and m, denoted by S(i, j, m), is specified as follows

$$S(i,j,m) = [w \times g(m) \times F(i,j)] \frac{\hat{\sigma}_i}{\hat{\sigma}_j},$$
(3)

where

$$F(i,j) = \begin{cases} 1 \text{ if } i = j \\ k_{ij} \text{ otherwise, } 0 \le k_{ij} \le 1 \end{cases}$$

$$\tag{4}$$

is the tightness of variable j in equation i relative to variable i and by increasing the interaction, i.e. it is possible for the value of k_{ij} to loosen the prior (Dua and Ray, 1995). The ratio $\frac{\hat{\sigma}_i}{\hat{\sigma}_j}$ consists of estimated standard errors of the univariate autoregression, for variables i and j. This ratio scales the variables to account for differences in the units of measurement, without taking into account the magnitudes of the variables. The term w measures the standard deviation on the first lag, and also indicates the overall tightness. A decrease in the value of w results in a tighter prior. The function $g(m) = m^{-d}$, d > 0 is the measurement of the tightness on lag m relative to lag 1, and is assumed to have a harmonic shape with a decay of d, which tightens the prior on increasing lags. Following the standard Minnesota prior settings, we choose the overall tightness (w) to be equal to 0.3, while the lag decay (d) is 1 and the interaction parameter (k_{ij}) is set equal to 0.5.

2.2 Factor Augmented VAR

Recently, Stock and Watson (2002), Forni and Reichlin (1996, 1998) and Forni *et al.* (1999, 2000) have shown that very large macroeconomic datasets can be properly modelled using dynamic factor models, where the factors can be considered as an "exhaustive summary of the information" in the data. The rationale underlying dynamic factor models is that the behavior of several variables is driven by few common forces, the factors, plus idiosyncratic shocks. Hence, the factors-approach can be useful in alleviating the omitted variable problem in empirical analysis using traditional small-scale models. Bernanke and Boivin (2003) and Bernanke *et al.* (2005) utilized factors in the estimation of VAR to

¹The basic principle behind the "Minnesota" prior is that all equations are centered around a random walk with drift. This idea has been modified by Kadiyala and Karlsson (1997) and Sims and Zha (1998). In Ingram and Whiteman (1994), a real business cycle model is used to generate a prior for a reduced form VAR, as a development of the "Minnesota" priors procedure. Also, a prior is placed on the parameters of a simple linearized DSGE, which is then compared with a Bayesian VAR in a forecasting exercise. Smets and Wouters (2003) extend this to medium scale New Keynesian models used in policy analysis. This approach has the advantage of providing information about which behavioural mechanisms produce forecast error or policy scenarios. However, it seems that it often fails to empirically fit compared to models with no behavioural structure. In Del Negro and Schorfheide (2004) and Del Negro, Schorfheide, Smets and Wouters (2007), a DSGE prior is also developed for a VAR.

generate a more general specification. Chudik and Pesaran (2011) illustrated how a VAR augmented by factors could help in keeping the number of estimated parameters under control without loosing relevant information.

Let \mathbf{X}_t denote an $N \times 1$ vector of economic time series and \mathbf{Y}_t a vector of $M \times 1$ observable macroeconomic variables which are a subset of \mathbf{X}_t . In this context, most of the information contained in \mathbf{X}_t is captured by \mathbf{F}_t , a $k \times 1$ vector of unobserved factors. The factors are interpreted as an addition to the observed variables, as common forces driving the dynamics of the economy. The relation between the "informational" time series \mathbf{X}_t , the observed variables \mathbf{Y}_t and the factors \mathbf{F}_t is represented by the following dynamic factor model:

$$\mathbf{X}_t = \mathbf{\Lambda}^f \mathbf{F} + \mathbf{\Lambda}^y \mathbf{Y}_t + e_t \tag{5}$$

where $\mathbf{\Lambda}^{f}$ is a $N \times k$ matrix of factor loadings, $\mathbf{\Lambda}^{y}$ is a $N \times M$ matrix of coefficients that bridge the observable \mathbf{Y}_t and the macroeconomic dataset, and e_t is the vector of $N \times 1$ error terms. These terms are mean zero, normal distributed, and uncorrelated with a small cross-correlation. In fact, the estimator allows for some cross-correlation in e_t that must vanish as N goes to infinity. This representation nests also models where \mathbf{X}_t depends on lagged values of the factors (Stock and Watson, 2002). For the estimation of the FAVAR model equation (5), we follow the two-step principal components approach proposed by Bernanke et al. (2005). In the first step factors are obtained from the observation equation by imposing the orthogonality restriction $\mathbf{F}'\mathbf{F}/T = \mathbf{I}$. This implies that $\hat{\mathbf{F}} = \sqrt{T}\hat{\mathbf{G}}$, where $\hat{\mathbf{G}}$ are the eigenvectors corresponding to the K largest eigenvalues of \mathbf{XX}' , sorted in descending order. Stock and Watson (2002) showed that the factors can be consistently estimated by the first r principal components of \mathbf{X} , even in the presence of moderate changes in the loading matrix $\mathbf{\Lambda}$. For this result to hold it is important that the estimated number of factors, k, is larger or equal than the true number r. Bai and Ng (2000) proposed a set of selection criteria to choose k that are generalizations of the BIC and AIC criteria. In the second step, we estimate the FAVAR equation replacing \mathbf{F}_t by $\hat{\mathbf{F}}_t$. Following Bernanke et al. (2005), \mathbf{Y}_t is removed from the space covered by the principal components. In a recent paper, Boivin et al. (2009) impose the constraint that \mathbf{Y}_t is one of the common components in the first step, guaranteeing that the estimated latent factors \mathbf{F}_t recover the common dynamics which are not captured by \mathbf{Y}_t . The authors, comparing the two methodologies, concluded that the results are similar. As in Bernanke et al. (2005) we partition the matrix \mathbf{X}_t in two categories of information variables: slow-moving and fast-moving. Slow-moving variables (e.g., real variables such as wages or spending) do not respond contemporaneously to unanticipated changes in monetary policy, while fast-moving (e.g., interest rates) respond contemporaneously to monetary shocks. We proceed to extracting two factors from slow variables and one factor from fast variables and we call them respectively "slow factors" and "fast factor". As suggested by Bai and Ng (2000) we use information criteria to determine the number of factors but, as they are not so decisive, we limit the number of factors to three (two slows and one fast) to strike a balance between the variance of the original series explained by the principal components and the difference in the parameterization of the VAR and the FAVAR. It is also worth noting that the factors are not uniquely identified, but this is not a problem in our context because we will not attempt a structural interpretation of the estimated factors. Finally, having determined the number of factors, we specify a Factor Augmented VAR by considering only one-lag of the factors according to BIC criterion. The potential identification of the macroeconomic shocks can be performed according to Bernanke et al. (2005) using the Cholesky decomposition.

3 DSGE model with financial frictions

The model proposed is a simple DSGE model obtained as a special case of Smets and Wouters (2007) model. We augment the small scale DSGE model by financial frictions as shown in Del Negro and Schorfheide (2012), following the work of Bernanke *et al.* (1999) and Christiano *et al.* (2009). We maintain a simplified version of capital to introduce the concept of financial friction with a small scale DSGE model. We follow the approach proposed by Del Negro and Schorfheide (2012), in that we

detrend the non-stationary model variables by a stochastic trend rather than a determinist trend. Del Negro and Schorfheide (2012) propose this approach to express almost all equilibrium conditions in a way that encompasses both the trend-stationary total factor productivity process in Smets and Wouters (2007) as well as when the technology follows a unit root process.

Let \tilde{z}_t be the linearly detrended log productivity process which follows the autoregressive AR(1) law of motion as exogenous shock:

$$\tilde{z}_t = \rho_z \tilde{z}_{t-1} + \sigma_z \epsilon_{z,t},\tag{6}$$

where $\epsilon_{z,t}$ is iid standard normal. Equation (6) implies that the growth rate of the trend process evolves according to:

$$z_t = \ln(\frac{Z_t}{Z_{t-1}}) - \gamma = \frac{1}{1-\alpha}(\rho_z - 1)\widetilde{z}_{t-1} + \frac{1}{1-\alpha}\sigma_z\epsilon_{z,t}$$

since we detrend all non stationary variables by $Z_t = e^{\gamma t + \frac{1}{1-\alpha}\tilde{z}_t}$, where γ is the steady state growth rate of the economy. The consumption Euler equation takes the form:

$$c_t = E_t[c_{t+1} + z_{t+1}] - \frac{1}{\sigma_c}(R_t - E_t[\pi_{t+1}])$$
(7)

where c_t is consumption, R_t is the nominal interest rate, $R_t - E_t[\pi_{t+1}]$ is the riskless return, π_t is inflation and σ_c is the relative degree of risk aversion. In this model we do not assume investment, consequently the capital accumulation process is given:

$$k_t = k_{t-1} - z_t + \rho_\mu \mu_{t-1} + \sigma_\mu \epsilon_{\mu,t}$$

The arbitrage condition between the return to capital and the riskless rate is modified as proposed by Del Negro and Schorfheide (2012):

$$E[\widetilde{R}_{t+1}^k - R_t] = \zeta_{sp}(\overline{k}_t - n_t) + \widetilde{\sigma}_{\omega,t}$$

and

$$\widetilde{R}_{t}^{k} - \pi_{t} = \frac{r_{*}^{k}}{r_{*}^{k} + (1 - \delta)} r_{*}^{k}$$
(8)

where r_*^k is the rental rate of capital of steady state, δ is the depreciation rate, \tilde{R}_t^k is the gross nominal return on capital for entrepreneurs, n_t is entrepreneurial equity which depends on equation (8) and $\tilde{\sigma}_{\omega,t}$ captures mean-preserving changes in the cross-sectional dispersion of ability across entrepreneurs (Christiano *et al.*, 2009) and follows an AR(1) process with parameters $\rho_{\sigma\omega}$ and $\sigma_{\sigma\omega}$. The first condition determines the spread between the expected return on capital and the riskless rate (if $\zeta_{sp} = 0$, the financial friction shocks are zero), while the second condition defines the return on capital. Capital is subject to variable capacity utilization u_t . The relationship between \overline{k}_t and the amount of capital effectively rented out to firms k_t is:

$$k_t = u_t - z_t + \overline{k}_{t-1}$$

The optimality condition determining the rate of utilization is given by:

$$\frac{1-\psi}{\psi}r_t^k = u_t$$

where ψ captures the utilization costs in terms of foregone consumption. From the optimality conditions of goods producers it follows that all firms have the same capital-labor ratio:

$$k_t = w_t - r_t^k + L_t$$

The real marginal costs are given by:

$$mc_t = w_t + \alpha L_t - \alpha k_t$$

where α is the income share of capital in the production.

The Phillips curve takes the form:

$$\pi_{t} = \frac{(1 - \zeta_{p}\beta)(1 - \zeta_{p})}{(1 + \iota_{p}\beta)\zeta_{p}}mc_{t} + \frac{\beta}{1 + \iota_{p}\beta}E_{t}[\pi_{t+1}] + \frac{\iota_{p}}{1 + \iota_{p}\beta}\pi_{t-1}$$
(9)

where ζ_p , and ι_p are the Calvo parameter and the degree of indexation. We assume that the central bank only reacts to inflation and output growth and that the monetary policy shock is iid. The policy rule is:

$$R_t = \rho_R R_{t-1} + (1 - \rho_R) \left[\psi_1 \pi_t + \psi_2 (y_t - y_{t-1} + z_t) \right] + \sigma_R \epsilon_{R,t}$$
(10)

where $\epsilon_{R,t}$ is iid standard normal. The aggregate resource constraint is:

$$y_t = c_t + g_t + k_t$$

where g_t is an exogenous shock process, evolving such as an AR(1):

$$g_t = \rho_g g_{t-1} + \sigma_g \epsilon_{g,t}$$

and $\epsilon_{g,t}$ is iid standard normal.

The previous set of equations can be recasted into a set of matrices $(\Gamma_0, \Gamma_1, C, \Psi, \Pi)$ accordingly to the definition of the vectors \tilde{Z}_t and ϵ_t

$$\Gamma_0 \ddot{Z}_t = C + \Gamma_1 \ddot{Z}_{t-1} + \Psi \epsilon_t + \Pi \eta_t \tag{11}$$

where η_{t+1} , such that $E_t \eta_{t+1} \equiv E_t (y_{t+1} - E_t y_{t+1}) = 0$, is the expectations error. As a solution to (11), we obtain the following transition equation as a policy function

$$\tilde{Z}_{t} = T\left(\theta\right)\tilde{Z}_{t-1} + R\left(\theta\right)\epsilon_{t} \tag{12}$$

and in order to provide the mapping between the observable data and those computed as deviations from the steady state of the model. The small-scale model is estimated based on four quarterly macroeconomic time series: The measurement equations for real output growth, inflation, short term interest rate and spread:

$$\Delta \ln x_t = \ln \gamma + \Delta \tilde{x}_t + \tilde{z}_t$$

$$\Delta \ln P_t = \ln \pi^* + \tilde{\pi}_t$$

$$\ln R_t^a = 4 \left[(\ln r^* + \ln \pi^*) + \tilde{R}_t \right]$$

$$SP_t = SP_* + 100 E_t [\tilde{R}_{t+1}^k - R_t]$$
(13)

where all variables are measured in percent and π_* , R_* and SP_* measure the steady state level of inflation, short term interest rate and spread. This can be also casted into matrices as

$$Y_t = \Lambda_0\left(\theta\right) + \Lambda_1\left(\theta\right)\ddot{Z}_t + v_t \tag{14}$$

where $Y_t = (\Delta \ln x_t, \Delta \ln P_t, \ln R_t, SP_t)'$, $v_t = 0$ and Λ_0 and Λ_1 are defined accordingly. For completeness, we write the matrices T, R, Λ_0 and Λ_1 as a function of the structural parameters in the model, θ . Such a formulation derives from the rational expectations solution. The evolution of the variables of interest, Y_t , is therefore determined by (12) and (14) which impose a set of restrictions across the parameters on the moving average (MA) representation. Given that the MA representation can be very closely approximated by a finite order VAR representation, Del Negro and Schorfheide (2004) propose to evaluate the DSGE model by assessing the validity of the restrictions imposed by such a model with respect to an unrestricted VAR representation. The choice of the variables to be included in the VAR is however completely driven by those entering in the DSGE model regardless of the statistical goodness of the unrestricted VAR.

3.1 Estimation of the linearized DSGE Model

Several econometric procedures have been proposed to parameterize and evaluate DSGE models. Kydland and Prescott (1982) use calibration, Christiano and Eichenbaum (1992) consider the generalized method of moments (GMM) estimation of equilibrium relationships, while Rotemberg and Woodford (1997) and Christiano *et al.* (2005) use the minimum distance estimation based on the discrepancy among VAR and DSGE model impulse response functions. Moreover the full-information likelihoodbased estimation is considered by Altug (1989), McGrattan (1994), Leeper and Sims (1994) and Kim (2000). In last years, Bayesian estimation became very popular. According to An and Schorfheide (2007) there are essentially three main characteristics. First, the Bayesian estimation is system-based and fits the solved DSGE model to a vector of aggregate time series, as opposed to the GMM which is based on equilibrium relationships, such as the Euler equation for the consumption or the monetary policy rule. Second, it is based on the likelihood function generated by the DSGE model rather than the discrepancy between DSGE responses and VAR impulse responses. Third, prior distributions can be used to incorporate additional information into the parameter estimation.

Priors distributions are important to estimate DSGE models. According to An and Schorfheide (2007) priors might downweigh regions of the parameter space that are at odds with observations which are not contained in the estimation sample. Priors could add curvature to a likelihood function that is (nearly) flat for some parameters, given a strong influence to the shape of the posterior distribution. Table 1 lists the prior distributions for the structural parameters of the DSGE model which are adopted from Del Negro and Schorfheide (2012).

In the Bayesian framework, the likelihood function is reweighted by a prior density. The prior is useful to add information which is contained in the estimation sample. Since priors are always subject to revisions, the shift from prior to posterior distribution can be considered as an indicator of the different sources of information. If the likelihood function peaks at a value that is at odds with the information that has been used to construct the prior distribution, then the marginal data density (MDD) of the DSGE model is defined as:

$$p(Y) = \int L(\theta|Y)p(\theta)d\theta$$

The marginal data density is the integral of the likelihood $(L(\theta|Y))$ taken according to the prior distribution $(p(\theta))$, that is the weighted average of likelihood where the weights are given by priors. The MDD can be used to compare different models M_i , $p(Y|M_i)$. We can rewrite the log-marginal data density as:

$$\ln(p(Y|M) = \sum_{t=1}^{T} \ln p(y_t|Y^{t-1}, M) =$$

=
$$\sum_{t=1}^{T} \ln \left[\int p(y_t|Y^{t-1}, \theta, M) p(\theta|Y^{t-1}, M) d\theta \right]$$

where $\ln(p(Y|M))$ can be interpreted as a predictive score (Good, 1952) and the model comparison based on posterior odds captures the relative one-step-ahead predictive performance. To compute the

Name	Density	Mean	Standard deviation			
Policy Parameters						
ψ_1	Gamma	1.500	0.250			
ψ_2	Gamma	0.120	0.050			
ρ_R	Beta	0.750	0.100			
	Norm	al Rigidit	ies Parameters			
ς_p	Beta	0.500	0.100			
Other 1	Endogenous Pr	opagation	and Steady State Parameters			
α	Normal	0.300	0.050			
ι_p	Beta	0.500	0.150			
$\dot{r_*}$	Gamma	0.250	0.100			
π_*	Gamma	0.620	0.100			
γ	Normal	0.400	0.100			
σ_c	Normal	1.500	0.370			
ψ	Beta	0.50	0.150			
ρ_z	Beta	0.500	0.200			
ρ_{μ}	Beta	0.500	0.200			
ρ_{a}	Beta	0.500	0.200			
σ_Z	Inv.Gamma	0.100	2.000			
σ_{μ}	Inv.Gamma	0.100	2.000			
σ_{g}	Inv.Gamma	0.875	0.430			
]	Financial	Frictions			
SP_*	Gamma	2.000	0.100			
$\rho_{\sigma\omega}$	Beta	0.750	0.150			
ς_{sp}	Beta	0.050	0.005			
$\sigma_{\sigma\omega}$	Inv.Gamma	0.050	4.000			

Table 1: Prior Distributions for the DSGE model parameters

Note: The model parameters are fixed in Del Negro and Schorfheide (2012): $\delta = 0.025$, and $g_* = 0.18$. The Inverse Gamma priors are of the form $p(\sigma|\nu, s) \propto \sigma^{-\nu-1} e^{-\nu s^2/2\sigma^2}$, where v=4 and s equals 0.2, 0.5, and 0.7, respectively. Approximately 1.5% of the prior mass lies in the indeterminacy region of the parameter space. The prior is truncated to restrict it to the determinacy region of the DSGE model, to avoid multiple equilibria typical in rational expectations models .

MDD, we consider the Geweke (1999) modified harmonic mean estimator. Harmonic mean estimators are based on the identity:

$$\frac{1}{p(Y)} = \int \frac{f(\theta)}{L(\theta|Y)p(\theta)} p(\theta|Y) d\theta$$

where $f(\theta)$ has the property that $\int f(\theta) d\theta = 1$ (Gelfand and Dey, 1994). Conditional on the choice of $f(\theta)$, an estimator is:

$$\widehat{p}_{G}(Y) = \left[\frac{1}{n_{sim}} \sum_{s=1}^{n_{sim}} \frac{f(\theta^{(s)})}{L(\theta^{(s)}|Y)p(\theta^{(s)})}\right]^{-1}$$
(15)

where $\theta^{(s)}$ is drawn from the posterior $p(\theta|Y)$. For a numerical approximation efficient, $f(\theta)$ should be chosen so that the summands are of equal magnitude. Geweke (1999) proposed to use the density of a truncated multivariate normal distribution:

$$f(\theta) = \tau^{-1}(2\pi)^{-\frac{d}{2}} |V_{\theta}|^{-\frac{1}{2}} \exp\left[-0.5(\theta - \overline{\theta})' V_{\theta}^{-1}(\theta - \overline{\theta})\right] \\ \times I\left\{(\theta - \overline{\theta})' V_{\theta}^{-1}(\theta - \overline{\theta}) \le F_{\chi_{d}^{2}}^{-1}(\tau\tau)\right\}$$

In the above $\overline{\theta}$ and V_{θ} are the posterior mean and covariance matrix computed from the output of the posterior simulator, d is the dimension of the parameter vector, $F_{\chi^2_d}$ is the cumulative density function of a χ^2 random variable with d degrees of freedom, and $\tau \in (0, 1)$. If the posterior of θ is in fact normal then the summands in eq. (15) are approximately constant.

3.2 The Del Negro-Schorfheide DSGE-VAR

Based on the study of Ingram and Whiteman (1994), Del Negro and Schorfheide (2004) designed the DSGE-VAR approach to improve forecasting and monetary policy analysis with VARs. Del Negro-Schorfheide's (2004) approach is to use the DSGE model to build prior distributions for the VAR. Basically, the estimation initializes with an unrestricted VAR of order p

$$\mathbf{Y}_t = \mathbf{\Phi}_0 + \mathbf{\Phi}_1 \mathbf{Y}_{t-1} + \dots + \mathbf{\Phi}_p \mathbf{Y}_{t-p} + \mathbf{u}_t \tag{16}$$

In compact format:

$$\mathbf{Y} = \mathbf{X}\mathbf{\Phi} + \mathbf{U} \tag{17}$$

Y is a $(T \times n)$ matrix with rows Y'_t , **X** is a $(T \times k)$ matrix (k = 1 + np, p =number of lags) with rows $X'_t = [1, Y'_{t-1}, ..., Y'_{t-p}]$, **U** is a $(T \times n)$ matrix with rows u'_t and Φ is a $(k \times n) = [\Phi_0, \Phi_1, ..., \Phi_p]'$. The one-step-ahead forecast errors u_t have a multivariate normal distribution $N(0, \Sigma_u)$ conditional on past observations of Y. The log-likelihood function of the data is a function of Φ and Σ_u

$$L(\mathbf{Y}|\Phi,\Sigma_u) \propto |\Sigma_u|^{-\frac{T}{2}} \exp\left\{-\frac{1}{2}tr\left[\Sigma_u^{-1}\left(\mathbf{Y}'\mathbf{Y} - \boldsymbol{\Phi}'\mathbf{X}'\mathbf{Y} - \mathbf{Y}'\mathbf{X}\boldsymbol{\Phi} + \boldsymbol{\Phi}'\mathbf{X}'\mathbf{X}\boldsymbol{\Phi}\right)\right]\right\}$$
(18)

The prior distribution for the VAR parameters proposed by Del Negro and Schorfheide (2004) is based on the statistical representation of the DSGE model given by a VAR approximation. Let Γ_{xx}^* , Γ_{yy}^* , Γ_{xy}^* and Γ_{yx}^* be the theoretical second-order moments of the variables Y and X implied by the DSGE model, where

$$\Phi^*(\theta) = \Gamma_{xx}^{*-1}(\theta) \Gamma_{xy}^*(\theta)$$

$$\Sigma^*(\theta) = \Gamma_{yy}^*(\theta) - \Gamma_{yx}^*(\theta) \Gamma_{xx}^{*-1}(\theta) \Gamma_{xy}^*(\theta)$$
(19)

The moments are the dummy observation priors used in the mixture model. These vectors can be interpreted as the probability limits of the coefficients in a VAR estimated on the artificial observations generated by the DSGE model. Conditional on the vector of structural parameters in the DSGE model θ , the prior distributions for the VAR parameters $p(\Phi, \Sigma_u | \theta)$ are of the Inverted-Wishart (IW) and Normal forms

$$\Sigma_{u} | \theta \sim IW \left((\lambda T \Sigma_{u}^{*}(\theta), \lambda T - k, n) \right. \\ \Phi | \Sigma_{u}, \theta \sim N \left(\Phi^{*}(\theta), \Sigma_{u} \otimes (\lambda T \Gamma_{XX}(\theta))^{-1} \right)$$
(20)

where the parameter λ controls the degree of model misspecification with respect to the VAR: for small values of λ the discrepancy between the VAR and the DSGE-VAR is large and a sizeable distance is generated between the unrestricted VAR and DSGE estimators. Large values of λ correspond to small model misspecification and for $\lambda = \infty$ beliefs about DSGE misspecification degenerate to a point mass at zero. Bayesian estimation could be interpreted as estimation based on a sample in which data are augmented by a hypothetical sample in which observations are generated by the DSGE model, the so-called dummy prior observations (Theil and Goldberg, 1961; Ingram and Whiteman, 1994). Within

this framework λ determines the length of the hypothetical sample. The posterior distributions of the VAR parameters are also of the Inverted-Wishart and Normal forms. Given the prior distribution, posterior distributions are derived by the Bayes theorem

$$\Sigma_{u} | \theta, \mathbf{Y} \sim IW\left((\lambda + 1) T \hat{\Sigma}_{u,b} (\theta), (\lambda + 1) T - k, n \right)$$
(21)

$$\boldsymbol{\Phi} \left| \Sigma_{u}, \theta, \mathbf{Y} \right| \sim N \left(\hat{\boldsymbol{\Phi}}_{b} \left(\theta \right), \Sigma_{u} \otimes \left[\lambda T \Gamma_{XX} \left(\theta \right) + \mathbf{X}' \mathbf{X} \right]^{-1} \right)$$
(22)

$$\hat{\boldsymbol{\Phi}}_{b}\left(\boldsymbol{\theta}\right) = \left(\lambda T \Gamma_{XX}\left(\boldsymbol{\theta}\right) + \mathbf{X}'\mathbf{X}\right)^{-1} \left(\lambda T \Gamma_{XY}\left(\boldsymbol{\theta}\right) + \mathbf{X}'\mathbf{Y}\right)$$
(23)

$$\hat{\Sigma}_{u,b}\left(\theta\right) = \frac{1}{\left(\lambda+1\right)T} \left[\left(\lambda T \Gamma_{YY}\left(\theta\right) + \mathbf{Y}'\mathbf{Y}\right) - \left(\lambda T \Gamma_{XY}\left(\theta\right) + \mathbf{X}'\mathbf{Y}\right)\hat{\mathbf{\Phi}}_{b}\left(\theta\right) \right]$$
(24)

where the matrices $\hat{\Phi}_b(\theta)$ and $\hat{\Sigma}_{u,b}(\theta)$ have the interpretation of maximum likelihood estimates of the VAR parameters based on the combined sample of actual observations and artificial observations generated by the DSGE. Equations (21) and (22) show that the smaller λ is, the closer the estimates are to the OLS estimates of an unrestricted VAR. Instead, the higher λ is, the closer the VAR estimates will be tilted towards the parameters in the VAR approximation of the DSGE model ($\hat{\Phi}_b(\theta)$ and $\hat{\Sigma}_{u,b}(\theta)$). In order to obtain a non-degenerate prior density (20), which is a necessary condition for the existence of a well-defined Inverse-Wishart distribution and for computing meaningful marginal likelihoods, λ has to be greater than λ_{MIN}

$$\lambda_{MIN} \geq \frac{n+k}{T}; k = 1 + p \times n$$

$$p = \text{lags}$$

$$n = \text{endogenous variables.}$$

Hence, the optimal lambda must be greater than or equal to the minimum lambda $(\hat{\lambda} \ge \lambda_{MIN})$. Essentially, the DSGE-VAR tool allows the econometrician to draw posterior inferences about the DSGE model parameters θ . Del Negro and Schorfheide (2004) explain that the posterior estimate of θ has the interpretation of a minimum-distance estimator, where the discrepancy between the OLS estimates of the unrestricted VAR parameters and the VAR representation of the DSGE model is a sort of distance function. The estimated posterior of parameter vector θ depends on the hyperparameter λ . When $\lambda \to 0$, in the posterior the parameters are not informative, so the DSGE model is of no use in explaining the data. Unfortunately, the posteriors (22) and (21) do not have a closed form and we need a numerical method to solve the problem. The posterior simulator used by Del Negro and Schorfheide (2004) is the Markov Chain Monte Carlo Method and the algorithm used is the Metropolis-Hastings acceptance method. This procedure generates a Markov Chain from the posterior distribution of θ and this Markov Chain is used for Monte Carlo simulations. The optimal λ is given by maximizing the log of the marginal data density

$$\hat{\lambda} = \operatorname*{arg\,max}_{\lambda \geqslant \lambda_{MIN}} \ln p(\mathbf{Y}|\lambda)$$

According to the optimal lambda $(\hat{\lambda})$, a corresponding optimal mixture model is chosen. This hybrid model is called DSGE-VAR $(\hat{\lambda})$ and $\hat{\lambda}$ is the weight of the priors. It can also be interpreted as the restriction of the theoretical model on the actual data.

3.3 Factor Augmented DSGE (DSGE-FAVAR)

Following Bernanke *et al.* (2005), a FAVAR benchmark for the evaluation of a DSGE model will include a vector of observable variables and a small vector of unobserved factors extracted from a large data-set of macroeconomic time series, that capture additional economic information relevant to model the dynamics of the observables. In this study we implement the DSGE-FAVAR model of Consolo *et al.* (2009). The statistical representation has the following specification:

$$\begin{pmatrix} \mathbf{Y}_t \\ \mathbf{F}_t \end{pmatrix} = \begin{bmatrix} \mathbf{\Phi}_{11}(L) & \mathbf{\Phi}_{12}(L) \\ \mathbf{\Phi}_{21}(L) & \mathbf{\Phi}_{22}(L) \end{bmatrix} \begin{pmatrix} \mathbf{Y}_{t-1} \\ \mathbf{F}_{t-1} \end{pmatrix} + \begin{pmatrix} \mathbf{u}_t^Y \\ \mathbf{u}_t^F \end{pmatrix}$$
(25)
$$\mathbf{Y}_t = (\Delta \ln x_t, \Delta \ln P_t, \ln R_t, SP_t)$$

$$\mathbf{F}_t = \begin{pmatrix} F_{1t}^s, F_{2t}^s, F_{3t}^f \end{pmatrix}$$

where \mathbf{Y}_t are the observable variables included in the simple DSGE model and \mathbf{F}_t is a small vector of unobserved factors relevant to modelling the dynamics of \mathbf{Y}_t (F_{1t}^s, F_{2t}^s are the two slow factors and F_{3t}^f is the fast factor). The system reduces to the standard VAR when $\Phi_{12}(L) = 0$. Importantly, and differently from Boivin and Giannoni (2006), this FAVAR is not interpreted as the reduced form of a DSGE model at hand. In fact, in this case the restrictions implied by the DSGE model on a general FAVAR are very difficult to trace and model evaluation becomes even more difficult to implement. A very tightly parameterized theory model can have a very highly parameterized reduced form if one is prepared to accept that the relevant theoretical concepts in the model are a combination of many macroeconomic and financial variables. The DSGE-FAVAR is implemented in the same way as the DSGE-VAR.

4 Empirical estimation

In this work we use quarterly data of the US economy from 1960:Q4 to 2010:Q4 with an out-of sample period that spans 1997:Q1 to 2010:Q4. The data for real output growth comes from the Bureau of Economic Analysis as Gross Domestic Product (GDP), while Consumer price index (CPI) data (seasonally adjusted, 1982-1984=100) are derived from the Bureau of Labor Statistics. Both series are taken in first difference logarithmic transformation. The interest rate series (FR rate) are constructed as in Clarida, Gah and Gertler (2000), namely for each quarter the interest rate is computed as the average federal funds rate during the first month of the quarter, including business days only. In the estimation of the DSGE model with financial frictions we measure the Spread as the annualized Moody's Seasoned BAA Corporate Bond Yield spread over the 10-Year Treasury Note Yield at Constant Maturity.

The complete dataset is used to extract factors for FAVAR and DSGE-FAVAR models. In order to construct the FAVAR we extract factors from a balanced panel of 109 monthly and quarterly macroeconomic and financial time series, following the dataset built by Stock and Watson (2002). The dataset involves several measures of industrial production, interest rates, various price indices, employment and other important macroeconomic and also financial variables. In this set-up, the number of informational time series N is large (larger than time period T) and must be greater than the number of factors and observed variables in the FAVAR system $(k + M \ll N)$. In the panel data used, there are some variables in monthly format, which are transformed into a quarterly data using end-of-period observations. All series have been transformed to induce stationarity. The series are taken as levels or transformed into logarithms, first or second difference (in level or logarithms) according to series characteristics ². Following Bernanke *et al.* (2005), we partition the data into two categories of information variables: slow and fast. Slow-moving variables (e.g., wages or spending) do not respond contemporaneously to unanticipated changes in monetary policy, while fast-moving variables (e.g., asset prices and interest rates) do respond contemporaneously to monetary shocks.

²The Appendix contains a detailed description of all series and their corresponding transformations.

Then we extract two factors from the slow variables and one factor from the fast variables. The methodology implemented to extract the factors is principal components. Stock-Watson (1998) showed that factors can be consistently estimated by the first r principal components of a matrix X, even in the presence of moderate changes in the loading matrix Λ . For this result to hold it is important that the estimated number of factors k, is larger than or equal to the true number, r. Bai and Ng (2000) propose a set of selection criteria to choose k that are generalizations of the BIC and AIC criteria. As they suggest, we use information criteria to determine the number of factors but, as they are not so decisive, we limit the number of factors to three to strike a balance between the variation in the original series explained by the principal components and the difference in the parameterization of the VAR and the FAVAR. It is also worth noting that the factors are not uniquely identified, but this is not a problem in our context because we will not attempt a structural interpretation of the estimated factors.

We compare the out-of-sample forecasting performance of VAR models including BVAR and FAVAR and of the DSGE class including DSGE-VAR, DSGE-FAVAR, in terms of the Root Mean Squared Forecast Error (RMSE) for the optimal lag specifications (one to four) selected by the Schwartz Bayesian information criterion (SIC). More importantly, we compare the log of the marginal data densities (MDD). Based on the MDD a forecasting exercise is provided using a rolling procedure for h-stepsahead. The GDP, CPI, FR rate and SP forecasts are estimated for the out-of-sample testing period 1997:Q1 - 2010:Q4. The forecasting investigation for the quarterly US data is performed over the one-, two-, three- and four-quarter-ahead horizon with a rolling estimation sample, based on the works of Marcellino (2004) and Brüggemann et al. (2008) for datasets of quarterly frequency. In particular, the models are re-estimated each quarter over the forecast horizon to update the estimate of the coefficients, before producing the quarter-ahead forecasts. Finally, in order to evaluate the models' forecast accuracy, we use the cross-model test statistic of Diebold and Mariano (1995). In particular, the modified Diebold and Mariano test (MDM) proposed by Harvey, Leybourne and Newbold (1997) is applied. The application of the MDM test is required as the DM could be seriously over-sized when the prediction horizon increases.

Firstly, we report estimation results for the log of Marginal Data Density (MDD). In particular, following Del Negro and Schorfheide (2006) we adopt the MDD as a measure of model fit, which arises naturally in the computation of posterior model odds. The prior distribution for the DSGE model parameters (θ) , which are similar to the priors used by Del Negro and Schorfheide (2004), were already illustrated in Table 1. This MDD measure has two dimensions: goodness of in-sample fit on the one hand and a penalty for model complexity or degrees of freedom on the other hand. The DSGE-VAR and the DSGE-FAVAR are estimated with a different number of lags on the sample 1960:Q4 -1996:Q4. From 1997:Q1, we start our forecasting evaluation as implemented in Herbst and Schorfheide (2012). The parameter λ is chosen from a grid which is unbounded from above. In our empirical exercise, the log of the MDD is computed over a discrete interval, $\ln p(Y|\lambda, M)$. The minimum value, $\lambda_{\min} = \frac{n+k}{2}$, is model dependent and is related to the existence of a well-defined Inverse-Wishart distribution. For completeness, it is worth mentioning that $\lambda = 0$ refers to the VAR and the FAVAR model with no prior and it is not possible to compute the marginal likelihood in this particular case. Therefore, we can show the log of MDD for any value of λ larger than λ_{\min} . Importantly, λ_{\min} depends on the degrees of freedom in the VAR or FAVAR and therefore, given estimation on the same number of available observations, λ_{\min} for a DSGE-FAVAR will always be larger than λ_{\min} for a DSGE-VAR³.

Table 2 shows the main results related to the DSGE-VAR implemented using a different number of lags (from 1 up to 4). Each minimum λ (λ_{MIN}) is given by the features of the model (number

 $[\]begin{array}{c} {}^{3} \mbox{ For the DSGE-VAR over the sample 1960:Q4-1996:Q4, the lambda grid is given by } \\ 0, 0.05, 0.08, 0.10, 0.12, 0.15, 0.20, 0.25, \\ 0.30, 0.35, 0.40 \ 0.5, 0.6, 0.7, 0.8, 0.9, 1, 10, 100 \end{array} \right\} . \\ \mbox{For the DSGE-FAVAR over the sample 1960:Q4-1996:Q4, the lambda grid is given by } \\ 0, 0.08, 0.1, 0.12, 0.14, 0.15, 0.2, 0.25, \\ 0.3, 0,35, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1, 10, 100 \end{array} \right\} . \\ \mbox{In both lambda intervals, we consider the λ_{MIN} across lags from 1 to 4. } }$

	λ_{MIN}	$\hat{\lambda}$	$\hat{\lambda} - \lambda_{MIN}$	$\frac{\hat{\lambda} - \lambda_{MIN}}{\lambda_{MIN}}$	$\ln p(Y \hat{\lambda}, M)$	Bayes Factor vs M_1
DSGE-VAR(1)	0.06	0.15	0.09	1.5	-671.626	exp[-1.468]
DSGE-VAR(2) (M_1)	0.09	0.15	0.06	0.66	-671.493	exp[-1.601]
DSGE-VAR(3)	0.11	0.20	0.09	0.82	-672.247	exp[-0.847]
DSGE-VAR(4)	0.14	0.25	0.11	0.79	-673.094	1
	λ_{MIN}	$\hat{\lambda}$	$\hat{\lambda} - \lambda_{MIN}$	$\frac{\hat{\lambda} - \lambda_{MIN}}{\lambda_{MIN}}$	$\ln p(Y \hat{\lambda},M)$	Bayes Factor vs $M_{\rm 2}$
DSGE-FAVAR (1)	0.08	0.10	0.02	0.25	-649.802	exp[15.078]
DSGE-FAVAR(2)	0.10	0.15	0.05	0.50	-642.442	exp[7.718]
DSGE-FAVAR (3)	0.12	0.20	0.08	0.66	-638.746	exp[4.022]
DSGE-FAVAR(4) (M_2)	0.15	0.25	0.10	0.66	-634.724	1

Table 2: Optimal lambda for the DSGE-VAR and DGSE-FAVAR calculated with Markov Chain Monte Carlo and Metropolis Hastings method

of observations, number of endogenous variables, number of lags), and the optimal lambda (λ) is calculated using the Markov Chain Monte Carlo with Metropolis Hastings acceptance method (with 110,000 replications, we discard the first 10,000 ones). $\ln p(Y|M)$ is the log-MDD of the DSGE model specifications computed based on Geweke's (1999) modified harmonic mean estimator. The Bayes factor (ratio of posterior odds to prior odds), as in An and Schorfheide (2007) helps us to understand the improvement of the log-MDD of a specific model. We compare different models against the benchmark model (M) maximizing the MDD. According to Table 2, we select the DSGE-VAR with 2 lags for the full sample 1960-1996. We repeat our exercise for the DSGE-FAVAR. We select one lag for the factors and we implement - as in case of the DSGE-VAR, - the DSGE-FAVAR with a different number lags from 1 to 4. As Table 2 shows, the DSGE-FAVAR with 4 lags is chosen. In Table 3, we compare the logarithm of the MDD of the hybrid models, DSGE-VAR and DSGE-FAVAR against the DSGE, the Bayesian VAR, the VAR and the Factor Augmented VAR. The FAVAR with 4 lags shows the maximum MDD.

Table 3: Log of the Marginal Data Density and Bayes Factor for the sample 1960:Q4-1996:Q4

	lnp(Y M)
DSGE	-693.765
DSGE-VAR(2)	-671.493
DSGE-FAVAR(4)	-634.724
BVAR(1)	-688.878
BVAR(2)	-671.757
BVAR(3)	-657.057
BVAR(4)	-645.230
VAR(1)	-673.906
VAR(2)	-672.368
VAR(3)	-672.636
VAR(4)	-672.046
FAVAR(1)	-649.580
FAVAR(2)	-646.821
FAVAR(3)	-642.736
$\mathbf{FAVAR}(4)$	-639.839

Table 4 reports the RMSE for all models and variables. An exhaustive exercise was conducted on

VAR and BVAR models with one to four lags based on the Schwartz Bayesian information criterion (SIC). The results provide evidence that in general four lags is the optimal number for these models. Overall, the results from RMSE are in accordance with those from the MDD estimation. In particular, for the GDP series the BVAR model provides the lowest RMSE for the one-, two- and three-steps ahead while only for the four-quarters-ahead the FAVAR outperforms the other models. The next two best performers are the FAVAR and DSGE-VAR models. The VAR, DSGE and DSGE-FAVAR models present similar predictive performance and on average they generate the highest forecast errors. Next, in case of the CPI variable, the DSGE model with financial frictions clearly outperforms all other models for all steps-ahead. The simple VAR and the DSGE-FAVAR outrank with a few exceptions the other model classes. The FAVAR model seems slightly better than BVAR, whilst the DSGE-VAR provides with relatively high scores for the RMSE for all quarters-ahead. The results for the FF rate series provide further evidence of the superiority of the DSGE with financial frictions. Specifically, when comparing the RMSE scores of all model classes, the DSGE is consistently the best performer in each forecasting horizon. The next lowest error is produced by the VAR model for all quarters-ahead. The DSGE-FAVAR model is better than the other for all steps-ahead, while the BVAR provides with the highest error. Finally, for the spread variable SP the BVAR model outperforms all models for the first three steps-ahead, with the exception of the four-quarter forecast where the DSGE with financial frictions provides the lowest RMSE. Overall, the simple VAR shows the worst performance, whilst the DSGE-FAVAR underperforms relatively to the other models in one- and four-quarters ahead and the simple DSGE in the other two forecasting horizons.

		-			()	
	VAR	BVAR	FAVAR	DSGE	DSGE-VAR	DSGE-FAVAR
GDP						
1	0.734	0.729	0.730	0.739	0.731	0.737
2	0.743	0.734	0.735	0.755	0.738	0.747
3	0.739	0.731	0.732	0.754	0.734	0.743
4	0.737	0.737	0.735	0.754	0.741	0.745
CPI						
1	0.870	0.892	0.885	0.856	0.898	0.870
2	0.875	0.893	0.886	0.836	0.897	0.875
3	0.876	0.897	0.890	0.829	0.902	0.875
4	0.882	0.888	0.883	0.811	0.891	0.879
FFR						
1	3.753	3.992	3.954	3.694	3.977	3.821
2	3.725	4.009	3.962	3.515	3.968	3.791
3	3.845	4.127	4.085	3.594	4.105	3.909
4	4.034	4.178	4.146	3.775	4.180	4.057
SP						
1	1.261	1.216	1.221	1.243	1.221	1.250
2	1.305	1.249	1.255	1.297	1.264	1.296
3	1.308	1.253	1.259	1.304	1.261	1.298
4	1.283	1.250	1.257	1.240	1.252	1.279

Table 4: Root Mean Square Forecast Error (RMSE) for GDP, CPI, FFR and SP

In the next step, the Modified Diebold-Mariano (MDM) pairwise test is employed in order to evaluate the comparative forecast accuracy. The results are reported in Tables 5, 6, 7 and 8. The Modified

GDP		PER	IODS	
	1	2	3	4
VAR vs BVAR	1.090	1.946	1.305	0.058
VAR vs FAVAR	0.992	1.473	1.321	2.070
VAR vs DSGE	1.414	2.025	2.528	1.743
VAR vs DSGE-VAR	0.817	1.830	1.266	1.526
VAR vs DSGE-FAVAR	4.234	3.402	2.575	2.498
BVAR vs FAVAR	1.174	0.948	0.209	1.714
BVAR vs DSGE	2.298	3.212	2.265	1.778
BVAR vs DSGE-VAR	1.307	1.621	1.166	4.569
BVAR vs DSGE-FAVAR	1.663	2.373	1.577	2.835
FAVAR vs DSGE	2.273	3.222	2.254	2.119
FAVAR vs DSGE-VAR	0.974	1.425	1.098	2.844
FAVAR vs DSGE-FAVAR	1.599	2.389	1.591	2.573
DSGE vs DSGE-VAR	2.080	2.757	2.541	1.493
DSGE vs DSGE-FAVAR	0.625	1.279	1.964	0.862
DSGE-VAR vs DSGE-FAVAR	1.696	2.603	1.682	1.626

Table 5: Pairwise forecast comparison for the GDP with the Modified Diebold-Mariano test

Notes: The Modified Diebold-Mariano (1995) test is based on squared prediction errors and is distributed as Student with (T-1) degrees of freedom, where T the out-of-sample sample period. The reported numbers are the t-scores.

Diebold-Mariano test is based on the squared prediction errors. The MDM test statistics for GDP lead to a diverse and variant assessment of differential predictability, albeit many pairwise comparisons produce a statistically significant MDM score. It appears that no particular model consistently and comparatively outperforms any of the other in all steps-ahead, while the RMSE results for the BVAR are not consistently verified at the 10%, 5% or 1% level in all pairwise comparisons. Hence, in some pairs of the BVAR model (e.g., BVAR vs. DSGE in all steps-ahead, BVAR vs. DSGE-FAVAR for twoand four-steps ahead etc.) differential predictability is significant at the 1% level, yet for most others this is not corroborated by the results. Considering the other pairs, the VAR model produces a significant predictability compared to DSGE and DSGE-FAVAR, the FAVAR vs. DSGE and the DSGE vs. DSGE-VAR and DSGE-FAVAR. The other examined cases in this study for GDP show weak or no differential predictability. On the contrary for the CPI series, the DSGE model with financial frictions in any pair shows a distinctively significant predictability at 1% (or 5%) in all step-ahead forecasts. This is in accordance with the RMSE results and in favor of the superior predictability of the DSGE model. In fact, most models for all forecast horizons appear to have a significant pairwise predictability at 5% or 1% level. The only exception is the pair VAR vs. DSGE-FAVAR for all steps-ahead and the pairs VAR-BVAR and VAR-FAVAR for the long forecast horizon of four quarters and FAVAR vs. DSGE-FAVAR also in four-steps-ahead. Thus, based on the MDD, RMSE and MDM results it is evident that in case of CPI the DSGE set-up including financial frictions outperforms the other models. Similar conclusions emerge from the investigation of the pairwise forecast comparison in case of FF Rate series. In particular, the results are indicative of a consistent outranking classification of the DSGE model vs. other models for all forecasting horizons. The DSGE model with the spread proxy produced the lowest RMSE in a previous examination and in conjunction with the MDM results it is shown that it consistently outperforms any of the other models for all quarter-ahead forecasts, namely the differential predictability is strongly significant at 1% level. Finally, in case of the SP variable the MDM scores depict in the majority of cases a statistically significant pairwise forecastability, albeit with many exceptions especially for the longer horizon. More importantly, the BVAR model that provided with the best performance in terms of the RMSE in this case - as opposed to the GDP series - in all pairs presents a consistent assessment of differential predictability i.e., comparatively

outperforms any of the other in all steps-ahead. However, the examination of other pairs is not indicative of statistically significant predictability. For example, VAR does not outperform the DSGE in any quarter-ahead forecast, the DSGE vs. DSGE-FAVAR pair is not producing significant scores even at the 10% level and the FAVAR is not comparatively different to the DSGE-FAVAR in almost all steps-ahead.

CPI		PERIODS				
	1	2	3	4		
VAR vs BVAR	4.659	2.910	2.702	1.673		
VAR vs FAVAR	4.090	2.245	2.282	0.488		
VAR vs DSGE	1.943	3.309	2.866	2.856		
VAR vs DSGE-VAR	4.906	3.034	2.803	1.943		
VAR vs DSGE-FAVAR	0.031	0.364	0.461	1.584		
BVAR vs FAVAR	5.375	4.662	4.182	4.056		
BVAR vs DSGE	3.596	3.799	3.239	3.011		
BVAR vs DSGE-VAR	5.554	2.694	3.136	2.173		
BVAR vs DSGE-FAVAR	5.118	3.145	3.024	2.319		
FAVAR vs DSGE	3.294	3.666	3.130	2.949		
FAVAR vs DSGE-VAR	5.615	4.052	3.703	3.095		
FAVAR vs DSGE-FAVAR	4.793	2.558	2.658	1.438		
DSGE vs DSGE-VAR	3.847	3.812	3.298	3.045		
DSGE vs DSGE-FAVAR	1.954	3.456	2.882	2.886		
DSGE-VAR vs DSGE-FAVAR	5.313	3.271	3.090	2.393		

Table 6: Pairwise forecast comparison for the CPI with the Modified Diebold-Mariano test

Notes: As in Table 5

5 Conclusions and policy implications

The financial crisis revealed that the workhorse of contemporary DSGE modelling is not fully ready to deal with the issue of credit frictions and financial stability, which play an important role in modern business cycle theory. Recently there have been some efforts to model financial factors mainly by Goodfriend and McCallum (2007), Christiano et al. (2010), Curdía and Woodford (2010), Gerali et al. (2010), Gertler and Kiyotaki (2010) and Gertler and Karadi (2011). These constitute some promising attempts to study the effects of financial intermediation on business cycle fluctuations and policy design. In particular, DSGE models with financial frictions could deal with many issues, such as the effect of financial shocks on real variables, how optimal monetary policy is affected by the presence of financial frictions and how macroprudential policies impact capital requirements. Moreover, new macroeconomic research is drawn to the application of Bayesian statistics because DSGE models are often seen as abstractions of actual economies. In this study we developed a DSGE model by augmenting the smallscale model with financial frictions, following Christiano et al. (2009) and Del Negro and Schorfheide (2012). In this way we investigated the response of the monetary policy to increase in interest rate spreads. We included a comparative evaluation of the out-of-sample predictive performance of many different specifications of estimated DSGE models and various classes of VAR models, using datasets from the US economy. Simple and hybrid DSGE models were implemented, such as DSGE-VARs and Factor Augmented DGSEs (DSGE-FAVAR), and tested against standard VARs, Bavesian VARs and Factor Augmented VARs (FAVAR). The results were evaluated with the use of Bayesian method

FFR	PERIODS				
	1	2	3	4	
VAR vs BVAR	6.541	3.564	2.916	2.176	
VAR vs FAVAR	6.485	3.464	2.863	2.022	
VAR vs DSGE	4.972	4.216	3.558	2.663	
VAR vs DSGE-VAR	6.407	3.641	2.924	2.324	
VAR vs DSGE-FAVAR	6.427	4.059	3.147	2.029	
BVAR vs FAVAR	6.802	4.116	3.229	2.842	
BVAR vs DSGE	7.658	4.847	3.952	3.098	
BVAR vs DSGE-VAR	4.450	2.651	2.045	0.387	
BVAR vs DSGE-FAVAR	6.527	3.389	2.815	2.103	
FAVAR vs DSGE	7.752	4.871	3.971	3.066	
FAVAR vs DSGE-VAR	4.489	0.758	2.063	3.508	
FAVAR vs DSGE-FAVAR	6.424	3.215	2.721	1.886	
DSGE vs DSGE-VAR	7.419	4.910	3.948	3.136	
DSGE vs DSGE-FAVAR	7.305	4.754	3.866	2.730	
DSGE-VAR vs DSGE-FAVAR	6.374	3.475	2.832	2.280	

Table 7: Pairwise forecast comparison for the FF rate with the Modified Diebold-Mariano test

Notes: As in Table 5

 Table 8: Pairwise forecast comparison for the SP with the Modified Diebold-Mariano test

SP	PERIODS					
	1	2	3	4		
VAR vs BVAR	6.645	4.102	3.177	2.875		
VAR vs FAVAR	6.289	3.884	2.991	2.596		
VAR vs DSGE	3.029	0.474	0.143	1.125		
VAR vs DSGE-VAR	6.990	4.204	3.310	2.872		
VAR vs DSGE-FAVAR	7.070	4.571	3.722	1.845		
BVAR vs FAVAR	4.546	3.107	2.580	2.443		
BVAR vs DSGE	4.131	2.683	2.053	0.323		
BVAR vs DSGE-VAR	3.522	3.148	2.004	1.187		
BVAR vs DSGE-FAVAR	6.496	3.963	3.052	2.731		
FAVAR vs DSGE	3.981	2.624	1.991	0.562		
FAVAR vs DSGE-VAR	0.357	1.816	0.398	1.508		
FAVAR vs DSGE-FAVAR	6.007	3.658	2.801	2.333		
DSGE vs DSGE-VAR	3.450	1.761	1.705	0.372		
DSGE vs DSGE-FAVAR	1.351	0.065	0.293	1.034		
DSGE-VAR vs DSGE-FAVAR	6.887	4.080	3.196	2.684		
Notes: As in Table 5						

of the marginal data density as well as the root mean squared forecast error. The modified Diebold and Mariano test (MDM) proposed by Harvey, Leybourne and Newbold (1997) was also employed to measure comparatively the differential forecastability taking into account the serious over-sizedness of the simple DM test when the prediction horizon increases. The best forecasting performance for the CPI and FF rate series was consistently produced by the DSGE model with financial frictions for all forecast horizons. For the GDP, the BVAR model provided with the most accurate forecasts up to three-quarters-ahead, whilst the FAVAR showed better predictability only for the longest horizon. Moreover, the BVAR model also outperformed all models in case of the SP financial variable with the exception of the four-quarter forecast where again the DSGE with financial frictions provided with the lowest RMSE. In general, FAVAR and DSGE-FAVAR were also good performers, whilst the other specifications provided with less satisfying forecasting results.

This work is open to several extensions. From the modelling point of view it should be relevant to focus on the interaction of frictions both at firms level and in the banking sector, in order to examine the transmission mechanism of the shocks and the accelerator/attenuator effects in line with the recent contribution by Rannenberg (2012). Moreover, the recent episodes of financial turmoil have reinforced the idea that the business cycle might be, to some extent, the result of changes in agents' expectations. Empirical evidence reported in Mankiw and Reis (2002), Orphanides and Williams (2008) and Lansing (2009) is in favour of the fact that expectations concerning inflation and other economic variables display systematic mistakes that increase the stochastic volatility in the economy. Further research is needed to find macro-financial models which are able to reflect reality better. For instance, featuring a more explicit modeling of financial intermediation or introducing occasionally binding constraints seem interesting avenues.

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6 Appendix

The source of the data is the Federal Reserve Economic Data - Federal Reserve Bank of Saint Louis (http://research.stlouisfed.org/fred2/). In order to construct the FAVAR we extract factors from a balanced panel of 109 monthly and quarterly macroeconomic and financial time series, following the dataset built by Stock and Watson (2002). The dataset involves several measures of industrial production, interest rates, various price indices, employment and other important macroeconomic and also financial variables. In the following Table, the first column has the series number, the second the series acronym, the third the series description, the fourth the transformation codes and the fifth column denotes a slow-moving variable with 1 and a fast-moving one with 0. The transformed series are tested using the Box-Jenkins procedure and the Dickey-Fuller test. Following Bernanke *et al.* (2005), the transformation codes are as follows: 1 - no transformation; 2 - first difference; 4 - logarithm; 5 - first difference of logarithm; 6 - second difference; 7 - second difference of logarithm.

Date	Long Description	Tcode	SlowCode
PAYEMS	Total Nonfarm Pavrolls: All Employees	5	1
DSPIC96	Real Disposable Personal Income	5	1
NAPM	ISM Manufacturing: PMI Composite Index	1	1
UNRATE	Civilian Unemployment Rate	1	1
INDPRO	Industrial Production Index (Index 2007=100)	5	1
PCEPI	Personal Consumption Expenditures: Chain-type Price Index (Index 2005=100)	5	1
PPIACO	Producer Price Index: All Commodities (Index 1982=100)	5	1
FEDFUNDS	Effective Federal Funds Rate	1	0
IPDCONGD	Industrial Production: Durable Consumer Goods (Index 2007=100)	5	1
IPBUSEQ	Industrial Production: Business Equipment (Index 2007=100)	5	1
IPMAT	Industrial Production: Materials (Index 2007=100)	5	1
IPCONGD	Industrial Production: Consumer Goods (Index 2007=100)	5	1
IPNCONGD	Industrial Production: Nondurable Consumer Goods (Index 2007=100)	5	1
IPFINAL	Industrial Production: Final Products (Market Group) (Index 2007=100)	5	1
UNEMPLOY	Unemployed	5	1
EMRATIO	Civilian Employment-Population Ratio (%)	1	1
CE16OV	Civilian Employment	5	1
CLF16OV	Civilian Labor Force	5	1
CIVPART	Civilian Participation Rate (%)	1	1
UEMP27OV	Civilians Unemployed for 27 Weeks and Over	5	1
UEMPLT5	Civilians Unemployed - Less Than 5 Weeks	5	1
UEMP15OV	Civilians Unemployed - 15 Weeks & Over	5	1
UEMP15T26	Civilians Unemployed for 15-26 Weeks	5	1
UEMP5TO14	Civilians Unemployed for 5-14 Weeks	5	1
MANEMP	Employees on Nonfarm Payrolls: Manufacturing	5	1
USPRIV	All Employees: Total Private Industries	5	1
USCONS	All Employees: Construction	5	1
USFIRE	All Employees: Financial Activities	5	1
USTRADE	All Employees: Retail Trade	5	1
DMANEMP	All Employees: Durable Goods Manufacturing	5	1
USGOOD	All Employees: Goods-Producing Industries	5	1
USEHS	All Employees: Education & Health Services	5	1
USLAH	All Employees: Leisure & Hospitality	5	1
SRVPRD	All Employees: Service-Providing Industries	5	1
USINFO	All Employees: Information Services	5	1
USPBS	All Employees: Professional & Business Services	5	1
USTPU	All Employees: Trade, Transportation & Utilities	5	1
NDMANEMP	All Employees: Nondurable Goods Manufacturing	5	1
USMINE	All Employees: Natural Resources & Mining	5	1
USWTRADE	All Employees: Wholesale Trade	5	1
USSERV	All Employees: Other Services	5	1
AHEMAN	Average Hourly Earnings: Manufacturing	5	1
AHECONS	Average Hourly Earnings: Construction (NSA)	5	1
PPIIDC	Producer Price Index: Industrial Commodities (NSA)	5	1

PPIFGS	Producer Price Index: Finished Goods (Index 1982=100)	5	1
PPICPE	Producer Price Index: Finished Goods: Capital Equipment (Index 1982=100)	5	1
PPICRM	Producer Price Index: Crude Materials for Further Processing (Index 1982=100)	5	1
PPIITM	Producer Price Index: Intermediate Materials: Supplies & Components (Index 1982=100)	5	1
PPIENG	Producer Price Index: Fuels & Related Products & Power (Index 1982=100)	5	1
PPIECG	Producer Price Index: Enisched Consumer Goods (Index 1982=100)	5	1
PECGEE	Producer Price Index: Finished Consumer Goods Excluding Goods (Index 1982=100)	5	1
CPIALICSI	Consumer Price Index for All Urban Consumers: All terms (Index 1982=100)	5	1
	Consumer Price Index for All Urban Consumers: All tems (Index 1982–190)	5	1
	Consumer Price Index for All Urban Consumers: All terms Lace Food & Energy (Index 10/2 84–100)	5	1
	Consumer Price Index for All Urban Consumers. All terms Less Food & Energy (INSA Index 1922–100)	5	1
	Consumer Price Index for All Urban Consumers: Food (NSA Index 1992=100)	5	1
CEICEDING	Consumer Price Index for All Obar Consumers, Food (NSA Index 1992 = 100)	5	4
	Consumer Price Index for All Urban Consumers: Energy (NSA Index 1982=100)	5 5	4
	Consumer Price Index for All Urban Consumers: Energy (Index 1962-1964=100)	5 5	4
	Consumer Price index for All Urban Consumers: All items Less Energy (index 1982-1984=100)	5 5	1
CPIMEDSL	Consumer Price Index for All Orban Consumers: Medical Care (Index 1982-1984=100)	5	1
PPIFCF	Producer Price Index: Finished Consumer Foods (Index 1982=100)	5	1
AAA	Moody's Seasoned Aaa Corporate Bond Yield	1	0
BAA	Moody's Seasoned Baa Corporate Bond Yield	1	0
M2SL	M2 Money Stock	6	0
M2NS	M2 Money Stock (NSA)	6	0
M1NS	M1 Money Stock (NSA)	6	0
M3SL	M3 Money Stock (DISCONTINUED SERIES)	6	0
GS5	5-Year Treasury Constant Maturity Rate	1	0
GS10	10-Year Treasury Constant Maturity Rate	1	0
GS1	1-Year Treasury Constant Maturity Rate	1	0
GS3	3-Year Treasury Constant Maturity Rate	1	0
TB3MS	3-Month Treasury Bill: Secondary Market Rate	1	0
TB6MS	6-Month Treasury Bill: Secondary Market Rate	1	0
HOUST	Housing Starts: Total: New Privately Owned Housing Units Started	5	0
PERMIT	New Private Housing Units Authorized by Building Permits	5	0
HOUSTMW	Housing Starts in Midwest Census Region	5	0
HOUSTW	Housing Starts in West Census Region	5	0
HOUSTNE	Housing Starts in Northeast Census Region	5	0
HOUSTS	Housing Starts in South Census Region	5	0
PERMITS	New Private Housing Units Authorized by Building Permits - South	5	0
PERMITMW	New Private Housing Units Authorized by Building Permits - Midwest	5	0
PERMITW	New Private Housing Units Authorized by Building Permits - West	5	0
PERMITNE	New Private Housing Units Authorized by Building Permits - Northeast	5	0
PDI	Personal Dividend Income	5	0
SPREAD1	3mo-FYFF	1	0
SPREAD2	6mo-FYFF	1	0
SPREAD3	1yr-FYFF	1	0
SPREAD4	2yr-FYFF	1	0
SPREAD5	3yr-FYFF	1	0
SPREAD6	5yr-FYFF	1	0
SPREAD7	7yr-FYFF	1	0
SPREAD8	10yr-FYFF	1	0
PCECC96	Real Personal Consumption Expenditures (Billions of Chained 2005 Dollars)	5	1
UNLPNBS	Nonfarm Business Sector: Unit Nonlabor Payments (Index 2005=100)	5	1
IPDNBS	Nonfarm Business Sector: Implicit Price Deflator (Index 2005=100)	5	1
OUTNFB	Nonfarm Business Sector: Output (Index 2005=100)	5	1
HOANBS	Nonfarm Business Sector: Hours of All Persons (Index 2005=100)	5	1
COMPNFB	Nonfarm Business Sector: Compensation Per Hour (Index 2005=100)	5	1
ULCNFB	Nonfarm Business Sector: Unit Labor Cost (Index 2005=100)	5	1
COMPRNFB	Nonfarm Business Sector: Real Compensation Per Hour (Index 2005=100)	5	1
OPHNFB	Nonfarm Business Sector: Output Per Hour of All Persons (Index 2005=100)	5	1
OPHPBS	Business Sector: Output Per Hour of All Persons (Index 2005=100)	5	1
ULCBS	Business Sector: Unit Labor Cost (Index 2005=100)	5	1
RCPHBS	Business Sector: Real Compensation Per Hour (Index 2005=100)	5	1
HCOMPBS	Business Sector: Compensation Per Hour (Index 2005=100)	5	1
OUTBS	Business Sector: Output (Ineex 2005=100)	5	1
HOABS	Business Sector: Hours of All Persons (Index 2005=100)	5	1
IPDBS	Business Sector: Implicit Price Deflator (Index 2005=100)	5	1
СР	Corporate Profits After Tax	5	0
SP500	S&P 500 Index	5	0